

# SINGLE-FIELD INFLATION MODELS IN SUPERGRAVITY

- $f(R)$  GRAVITY AS GRAVITY + SCALAR
- THE “STAROBINSKY” CASE  $f = R + \alpha R^2$
- $R^n$  CORRECTIONS
- $R + \alpha R^2$  SUPERGRAVITY AT LINEAR ORDER
- THE NEW MINIMAL SUPERGRAVITY
- NEW MINIMAL COMPLETION OF  $R + \alpha R^2$  GRAVITY
- HIGHER-CURVATURE CORRECTIONS
- NEW MINIMAL CHAOTIC INFLATION AND F TERMS

# BOSONIC HIGHER-CURVATURE GRAVITY

$$\text{SET } 8\pi G = 1$$

EINSTEIN ACTION PLUS HIGHER-CURVATURE  
CORRECTIONS

$$L = \frac{1}{2}R + f(R) = \frac{1}{2}R + f(X) + \frac{1}{2}Y(R - X)$$

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## RESCALE TO EINSTEIN FRAME

$$g_{mn} \rightarrow (1 + Y)^{-1} g_{mn}$$

$$(1 + Y)\sqrt{-g}R \rightarrow \sqrt{-g}R - \frac{3}{2}\sqrt{-g}[\partial_m \log(1 + Y)]^2$$

## THE LAGRANGIAN DENSITY BECOMES

$$L = \frac{1}{2}R - \frac{1}{2}(\partial_m \phi)^2 - (1 + Y)^{-2} \tilde{f}[Y(\phi)]$$

$$\phi = \sqrt{3/2} \log(1 + Y)$$

$$\tilde{f}(Y) = YX - f(X) \Big|_{f'(X)=Y}$$

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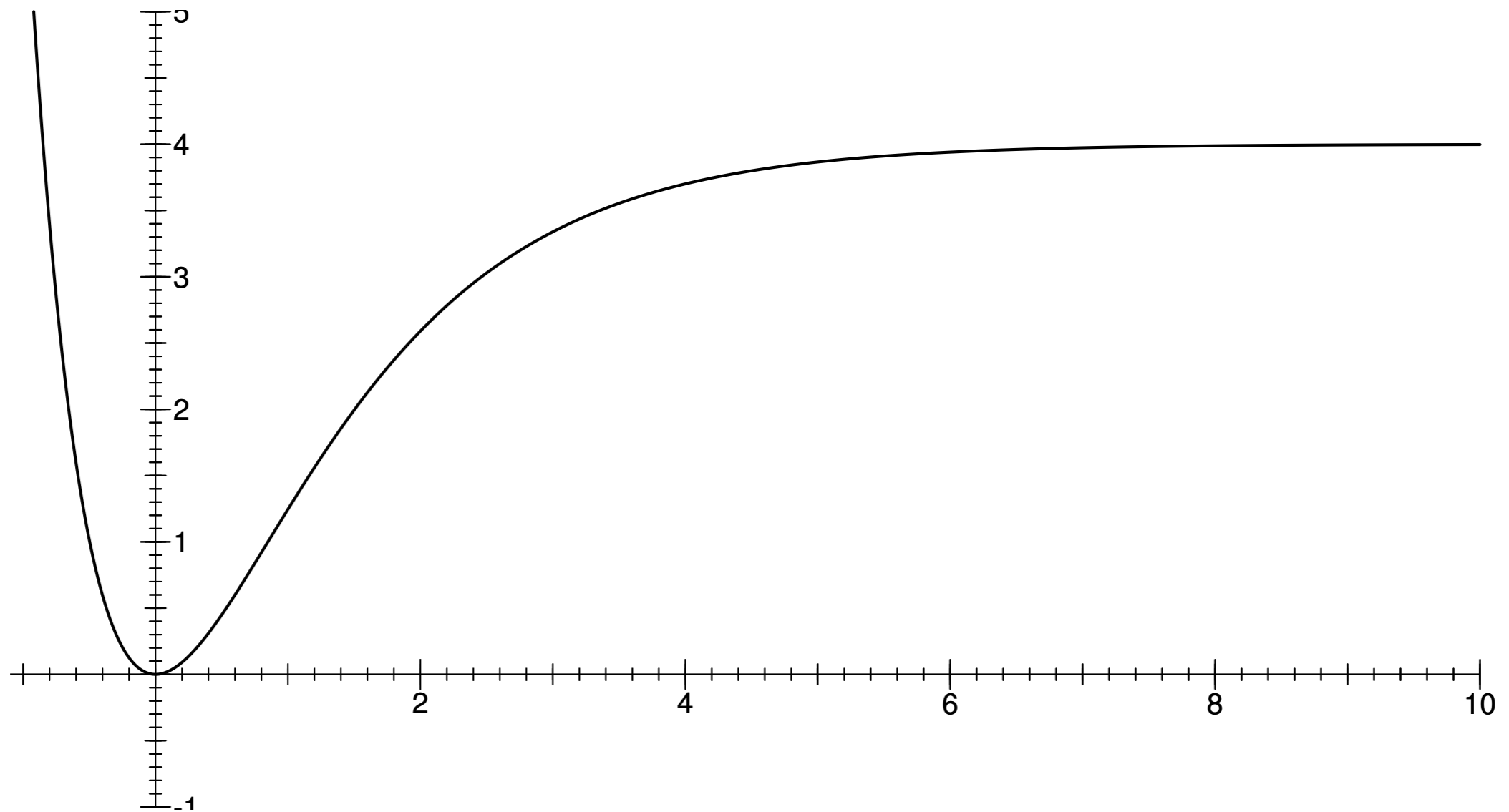
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## LEGENDRE TRANSFORM

IN PARTICULAR, WHEN  $f(X) = \frac{1}{2g^2} X^2$

THE POTENTIAL IS  $(1 + Y)^{-2} \tilde{f}(Y) = \frac{g^2}{2} \left(1 - e^{-\sqrt{2/3}\phi}\right)^2$

# THE “STAROBINSKY” POTENTIAL (VERTICAL AXIS SCALE MULTIPLIED BY $8/g^2$ )



# HIGHER ORDER CORRECTIONS: WHICH SCALE?

$$R + \frac{1}{2g^2}R^2 \rightarrow Rf(R/g^2), \quad f(x) = 1 + \frac{1}{2}x + O(1)x^4 + \dots$$

WHEN CURVATURE IS  $O(g^2)$  ALL TERMS ARE EQUAL

IS IT POSSIBLE TO GET ANOTHER FACTOR  $O(g^2)$

IN FRONT OF THE HIGHER CURVATURE CORRECTIONS?

WHAT ABOUT CHAOTIC INFLATION?

T.B.C.....

# SUPERSYMMETRIZATION OF $f(R)$ GRAVITY

- GRAVITON (OFF SHELL) DEGREES OF FREEDOM:  $10-4=6$
- GRAVITINO DEGREES OF FREEDOM  $16-4=12$
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- OLD MINIMAL:  $4+2$  DOF  $A_\mu, S + iP$
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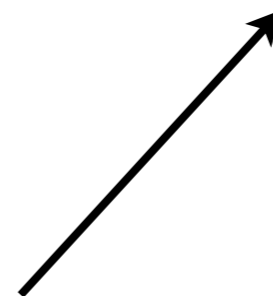
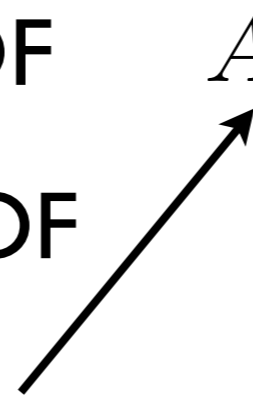
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GAUGE INVARIANCE  $B_{\mu\nu} \rightarrow B_{\mu\nu} + \partial_{[\mu}\xi_{\nu]}$ ,  $A_\mu \rightarrow A_\mu + \partial_\mu\xi$

OLD MINIMAL AND NEW MINIMAL DIFFER BY  
NON PROPAGATING DEGREES OF FREEDOM IN  
STANDARD "EINSTEIN" SUPERGRAVITY; WHEN  
HIGHER CURVATURE TERMS ARE INTRODUCED  
THEY AUXILIARY FIELDS PROPAGATE AND THE  
TWO FORMALISMS ARE NO LONGER EQUIVALENT

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ANALYSIS IN THE NEW MINIMAL FORMALISM: 1988,  
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IN OLD-MINIMAL, THE BOSONIC PART OF THE ACTION IS

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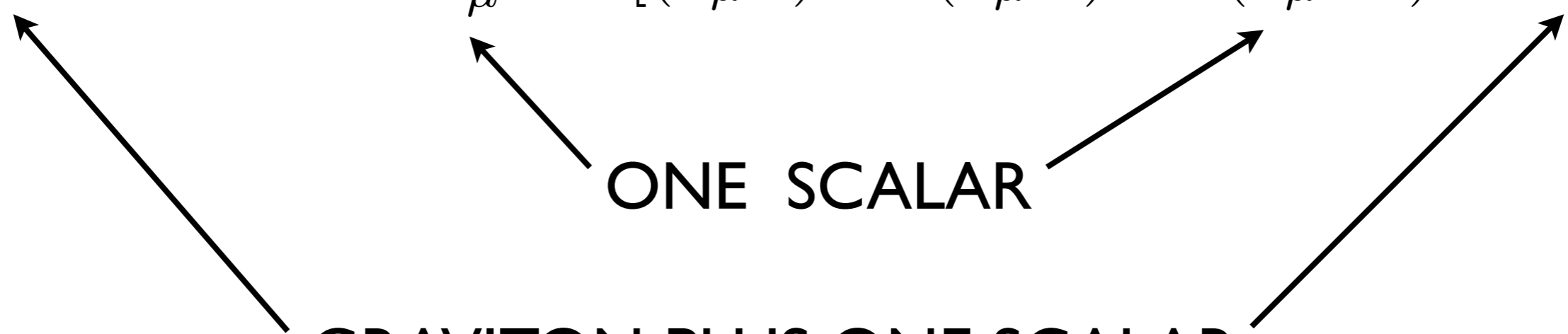
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ONE SCALAR

GRAVITON PLUS ONE SCALAR



THE OLD MINIMAL SUPERSYMMETRIZATION OF ACTIONS WITH HIGHER POWERS OF THE SCALAR CURVATURE CONTAINS FOUR SCALARS. IN THE SIMPLEST REALIZATIONS OF INFLATIONARY POTENTIALS THESE SCALARS MAY BECOME UNSTABLE DURING SLOW ROLL.

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THE SUPERMULTIPLY CONTAINING THE DEGREES OF FREEDOM RELEVANT TO A NEW MINIMAL SUPERSYMMETRIZATION OF ACTIONS WITH HIGHER POWERS OF THE SCALAR CURVATURE CAN BE WRITTEN AT THE FULL NON-LINEAR LEVEL USING SUPERCONFORMAL CALCULUS

# CONFORMAL CALCULUS: (ADD DILATON DOF AND WEYL INVARIANCE TO REMOVE IT)

$$g_{\mu\nu} \rightarrow \hat{g}_{\mu\nu} \equiv \phi^2 g_{\mu\nu} \text{ s.t. } g_{\mu\nu} \rightarrow \Omega^2 g_{\mu\nu}, \phi \rightarrow \Omega^{-1} \phi$$

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SUPERCONFORMAL CALCULUS: (ADD DILATON  
CHIRAL MULTIPLIET AND SUPER-WEYL  
INVARIANCE TO REMOVE IT)

THE BOSONIC PART OF SUPER-WEYL CONTAINS  
SCALE PLUS CHIRAL TRANSFORMATION: SUPER-  
WEYL MULTIPLIETS ARE CLASSIFIED BY CHARGE  
AND SCALING DIMENSION



THE NEW MINIMAL EINSTEIN ACTION DEPENDS  
ON A CHIRAL COMPENSATOR WITH  
(SCALING DIMENSION, CHIRAL WEIGHT)=(1, 1)  
AND A LINEAR MULTIPLY WITH WEIGHTS (2, 0)

$$\mathcal{L}_E = [LV_R]_D, \quad V_R = \log(L/S\bar{S})$$

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$$D^2 L = \bar{D}^2 L = 0 \rightarrow L = \dots + \bar{\theta}\sigma^\mu\theta A_\mu + \dots, \quad \partial_\mu A^\mu = 0$$

LINEAR MULTIPLER

THE ACTION IS INDEPENDENT OF THE CHIRAL COMPENSATOR BECAUSE IT CAN BE SCALED TO A CONSTANT WITH A GAUGE TRANSFORMATION PARAMETRIZED BY A CHIRAL SUPERFIELD

$$S \rightarrow S' = e^{\Omega} S, \quad S' = 1, \quad V_R \rightarrow V_R + \Omega + \bar{\Omega}$$

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HIGHER ORDER TERMS ARE WRITTEN IN TERMS OF THE GAUGE-INVARIANT FIELD STRENGTH

$$W_{\alpha}(V_R) = \bar{D}^2 D_{\alpha} V_R = \theta_{\alpha} R + \dots$$

# THE NEW MINIMAL $R + \alpha R^2$ ACTION

$$\mathcal{L} = [LV_R]_D + \frac{1}{2g^2} [W_\alpha^2(V_R)]_F + c.c.$$

$\theta^2$  TERM



THE ACTION IS DUAL TO A STANDARD SUPERGRAVITY ACTION DESCRIBING GRAVITON+GRAVITINO PLUS A MASSIVE VECTOR MULTIPLY [1,(2)1/2,0] (CECOTTI, FERRARA, M.P., SABHARWAL, 1988; RIOTTO, KEHAGIAS, 2013)

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TRICK: INTRODUCE AN UNCONSTRAINED REAL MULTIPLY AS LAGRANGE MULTIPLY:  $R$

$$\mathcal{L} = -[S\bar{S}e^U U]_D + [R(S\bar{S}e^U - L)]_D + \frac{1}{2g^2} [W_\alpha^2(U)]_F + c.c.$$

**ACTION DOES NOT DEPEND ON  $S$  BECAUSE OF GAUGE INVARIANCE**

$$S \rightarrow Se^Y, \quad U \rightarrow U - Y - \bar{Y}, \quad R \rightarrow R - Y - \bar{Y}$$



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$$R = T + \bar{T}$$

**REDEFINE**  $S \rightarrow Se^{-T}$

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**ACTION DESCRIBES A MASSIVE VECTOR MULTIPLY**

$$\mathcal{L} = -[S\bar{S}(U - T - \bar{T})e^{(U-T-\bar{T})}]_D + \frac{1}{2g^2} [W^2(U)]_F + c.c.$$

THIS IS A PARTICULAR CASE OF THE GENERAL N=1 ACTION  
WHERE THE U(1) GAUGED BY THE VECTOR FIELD IS IN THE  
BROKEN PHASE

$$U e^U \rightarrow e^{(2/3)J(U-T-\bar{T})}, \quad J(C) = \frac{3}{2}(C - \log C)$$

STUCKELBERG  
FIELD

KAEHLER POTENTIAL

$$T \rightarrow T + \Omega, \quad U \rightarrow U + \Omega + \bar{\Omega}$$

THE BOSONIC ACTION CAN BE COMPUTED  
USING THE GENERAL FORMULAS OF N=1  
SUPERGRAVITY

$$\mathcal{L} = \frac{1}{2}R - \frac{1}{2}J''(C)\partial_\mu C\partial^\mu C - \frac{1}{4g^2}F_{\mu\nu}(B)F^{\mu\nu}(B) - \frac{1}{2}J''(C)B_\mu B^\mu - \frac{g^2}{2}J'^2(C)$$

DEGREES OF FREEDOM: ONE SCALAR AND ONE MASSIVE  
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DEGREES OF FREEDOM: ONE SCALAR AND ONE MASSIVE  
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FOR THE KAEHLER FUNCTION  $J(C) = \frac{3}{2}(C - \log C)$

REDEFINE  $C = \exp(\sqrt{2/3}\phi)$

THE POTENTIAL IS  $V = \frac{9}{8}g^2(1 - e^{-\sqrt{2/3}\phi})^2$

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CHIRAL PROJECTOR

$$(w, w - 2) \xrightarrow{\Sigma} (w + 1, w + 1)$$

$$\mathcal{L} = [LV_R]_D + \frac{1}{2g^2} [W^2]_F + \sum_{klp} a_{klp} \left[ \frac{W^2 \bar{W}^2}{L^2} \left( \bar{\Sigma} \frac{W^2}{L^2} \right)^k \left( \Sigma \frac{\bar{W}^2}{L^2} \right)^l \left( \frac{D^\alpha W_\alpha}{L} \right)^p \right]_D$$



# THE BOSONIC ACTION CONTAINS THE TERMS

$$\mathcal{L} = \frac{1}{2}R + \frac{1}{18g^2}R^2 + \sum_{klp} a_{klp}R^{4+p+2k+2l}$$

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(ANTI) SELF-DUAL FIELD STRENGTH

AUXILIARY FIELD

## DANGEROUS CORRECTIONS:

$$a_{klp} \sim g^{-(6+4k+4l+2p)}$$

BECAUSE THE HIGHER-ORDER TERMS BECOME  $O(1)$  AT THE  
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BUT BEHAVIOR IS TOO SINGULAR IN THE “UNHIGGSED”  
LIMIT  $g \rightarrow 0$

NORMALIZE VECTOR FIELD

$$B_\mu \rightarrow gB_\mu$$

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**REGULARITY OF BORN-INFELD TERMS**

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E.G. DURING SLOW ROLL THE FIRST CORRECTION ( $R^4$ )  
IS AT MOST

$$g^{-4} R^4 \sim R^2 \ll \frac{1}{18g^2} R^2, \quad g \sim 10^{-4} - 10^{-5}$$



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- WE HAVE HERE A NEW SETTING FOR FINDING SUCH A POTENTIAL

$$J = C^2/2, \quad V = \frac{g^2}{2} C^2$$

# RATHER GENERAL COUPLING TO MATTER

$$\begin{aligned} \mathcal{L} = & -[S\bar{S}e^U (U + \Phi(U, Z, \bar{Z}))]_D + [R(S\bar{S}e^U - L)]_D \\ & + \frac{1}{2g^2} [W_\alpha^2(U)]_F + [S^3 W(Z)]_F + c.c. \end{aligned}$$

GAUGE INVARIANT UNDER

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SOLVE  $L$  E.O.M. GET STANDARD SUGRA  
LAGRANGIAN WITH (BROKEN) GAUGED R-SYMMETRY

# RATHER GENERAL COUPLING TO MATTER

$$\mathcal{L} = -[S\bar{S}e^U (U + \Phi(U, Z, \bar{Z}))]_D + [R(S\bar{S}e^U - L)]_D \\ + \frac{1}{2g^2} [W_\alpha^2(U)]_F + [S^3 W(Z)]_F + c.c.$$

GAUGE INVARIANT UNDER

$$Z^I \rightarrow e^{q_I \Omega} Z^I, \quad S \rightarrow S e^{-\Omega}, \quad U \rightarrow U + \Omega + \bar{\Omega}$$

CONSTRAINT  $R$  SAYS THAT  
COMPOSITE MULTIPLY  $V_R$  GAUGES THE R-SYMMETRY

SOLVE  $L$  E.O.M. GET STANDARD SUGRA  
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CFR. LUST-KOUNNAS-TOUMBAS arXiv: 1409.7076  
FERRARA-PORRATI arXiv: 1506.01566



# SCALAR POTENTIAL

A LOT OF CANCELATIONS LEAD TO

$$V = W_I \Phi^{I\bar{J}} \bar{W}_{\bar{J}} + \frac{g^2}{2} D^2$$

$$D = -6e^{-\sqrt{2/3}\phi} + 6 + \text{terms quadratic in matter fields } z$$

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# CONCLUSIONS

- INFLATIONARY  $f(R)$  SCENARIOS CAN BE EMBEDDED IN SUPERGRAVITY
- THE NEW MINIMAL FORMALISM IS PARTICULARLY SUITED TO STUDY  $f(R)$  THEORIES BECAUSE IT ADDS ONE SINGLE SCALAR TO THE GRAVITATIONAL SUPERMULTIPLY, WHICH IS UNEQUIVOCALLY IDENTIFIED WITH THE INFLATON
- POTENTIALLY DANGEROUS HIGHER-CURVATURE CORRECTIONS ARE FORBIDDEN BY A DECOUPLING ARGUMENT
- THE D-TERM POTENTIAL CAN BE EMBEDDED INTO A POTENTIAL CONTAINING D AND F TERMS

- **LAST BUT NOT LEAST: THE LAGRANGIAN DUAL TO NEW-MINIMAL HIGH CURVATURE POTENTIALS GIVES THE SIMPLEST AND MOST NATURAL REALIZATION IN SUPERGRAVITY OF QUADRATIC-POTENTIAL CHAOTIC INFLATION**