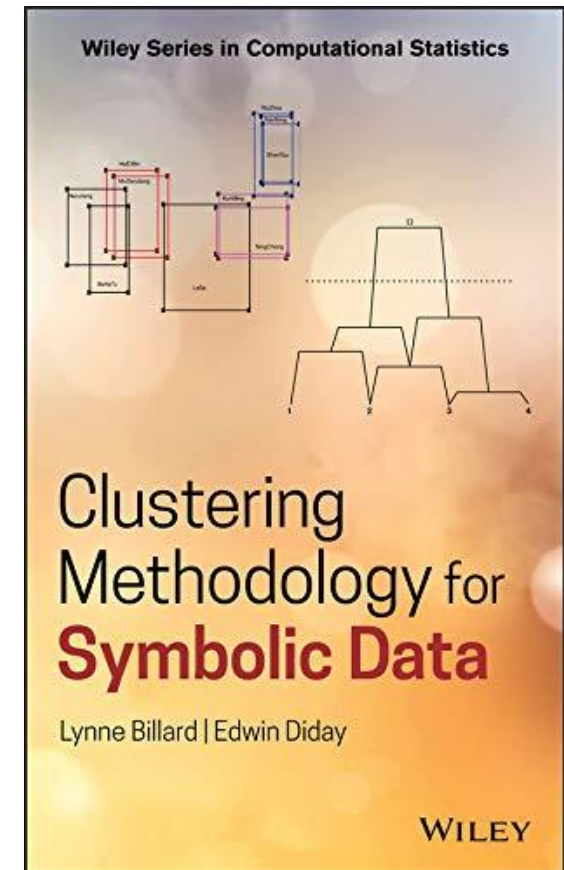
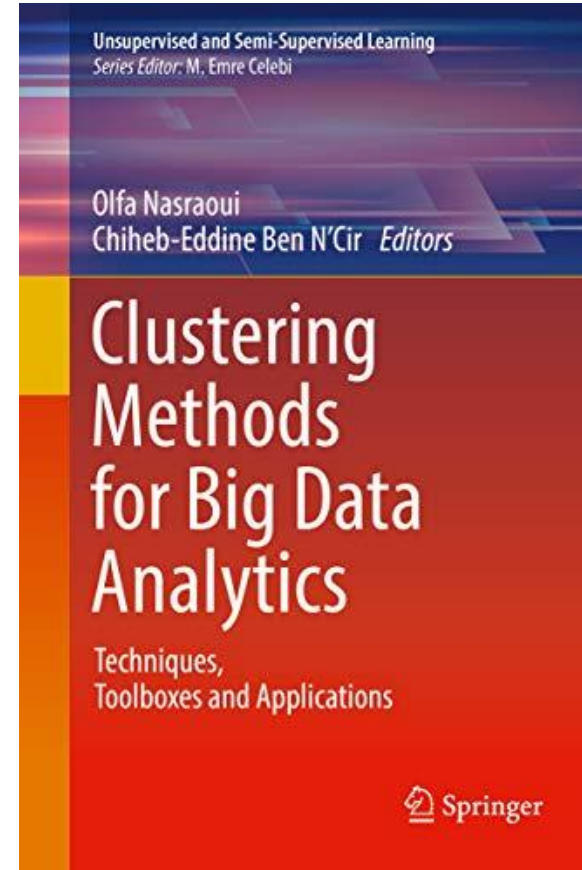
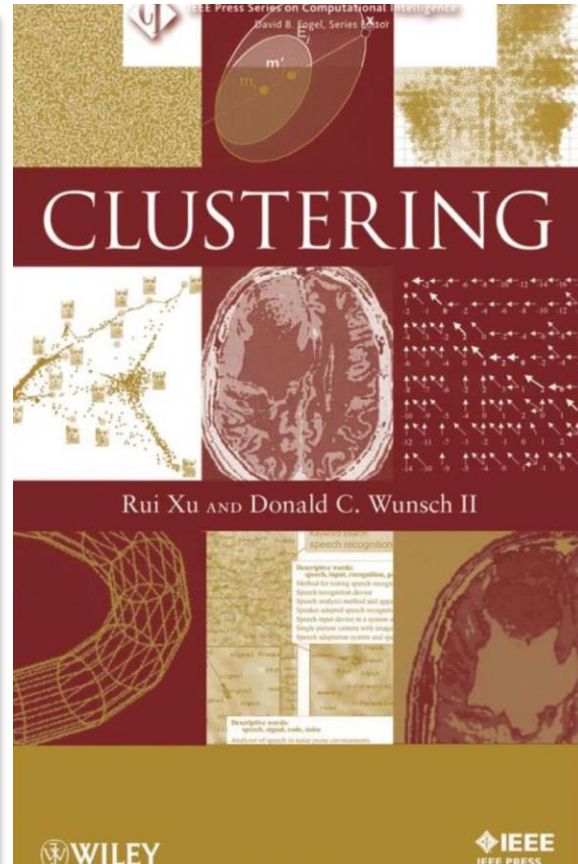
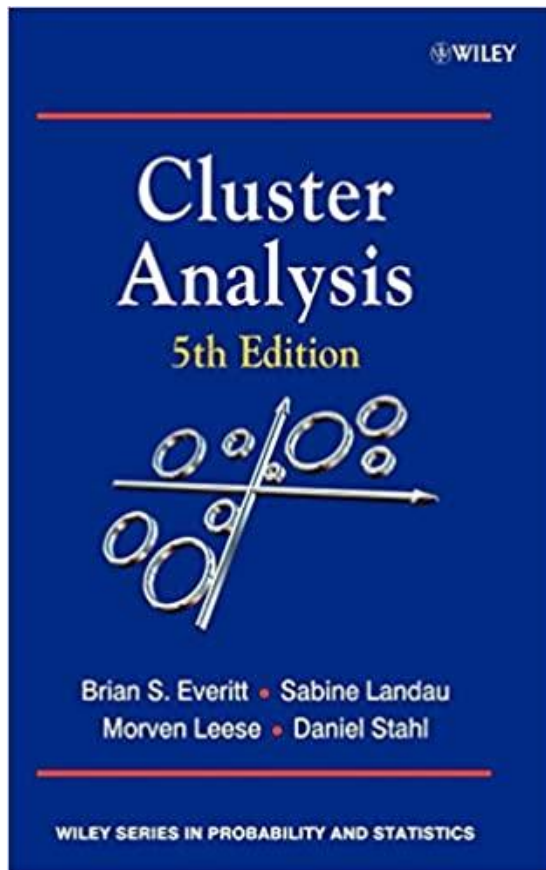


Fundamentals of AI

Clustering

General principles and classification of clustering methods

Some books



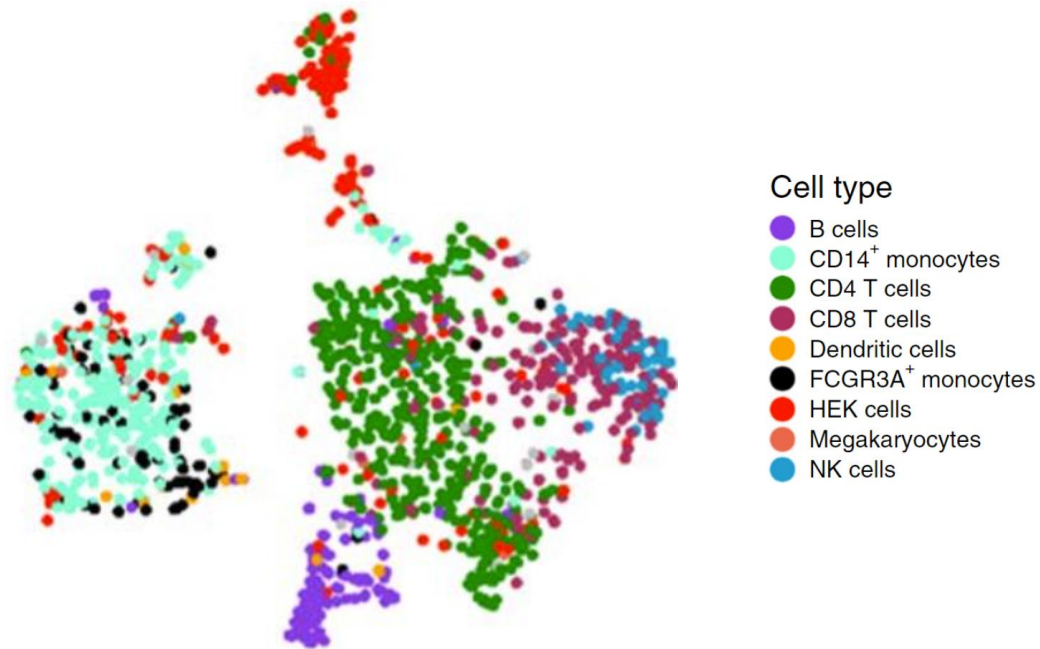
Clustering problem in machine learning

- Part of unsupervised classification and exploratory data analysis
- Pure case : no labeled data are available (Everitt et al., 2001 ; Jain and Dubes, 1988)
- The goal of clustering is to separate a finite, unlabeled data set into a finite and discrete set of “natural”, “hidden” data structures



Distinguish *classes* and *clusters*!!!

- **Class** = set of data points with the same pre-defined label
- **Cluster** = result of solving a clustering problem



From Mereu et al, Nature Biotech , 2020

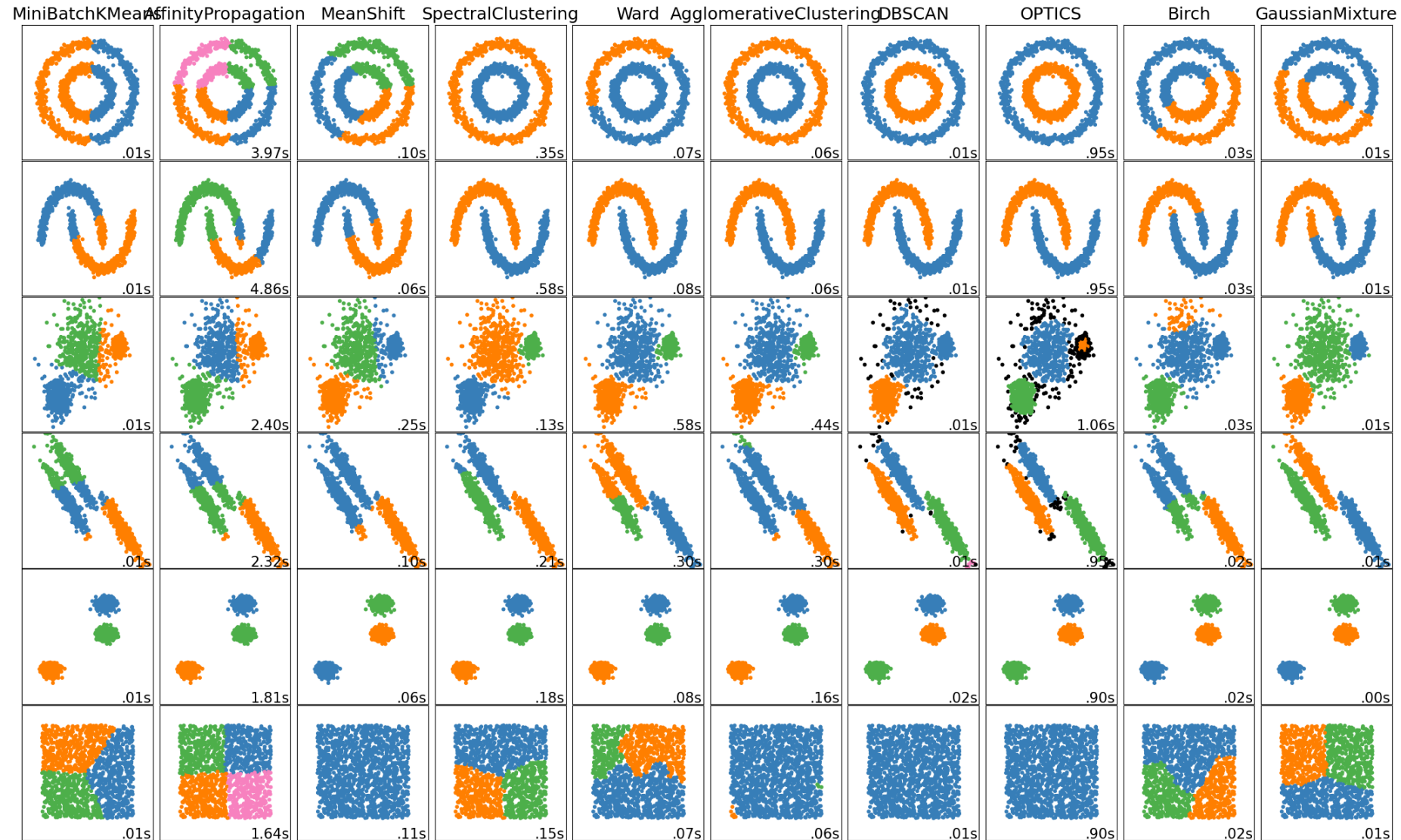
Example of complex clustering problem



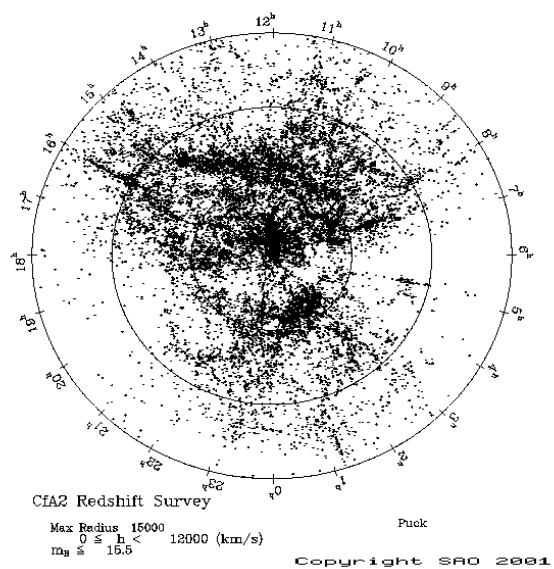
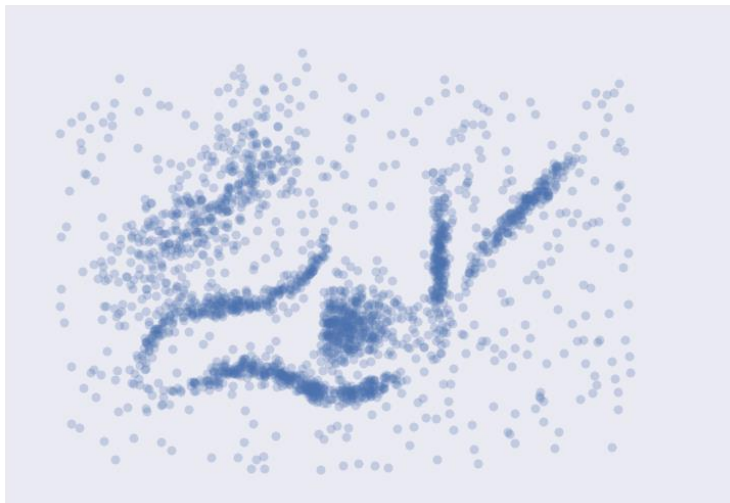
“Google cat”



Clustering in scikit-learn in 2D



What about this?



<https://amp.pharm.mssm.edu/archs4/data.html>

Immediate questions

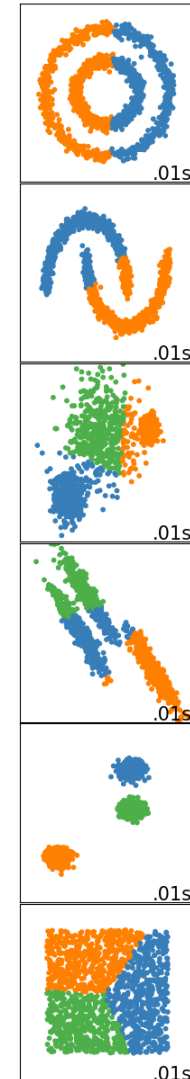
- What is cluster?
- How many clusters?
- Typology of cluster methods
- How to choose the best method?

What is cluster?

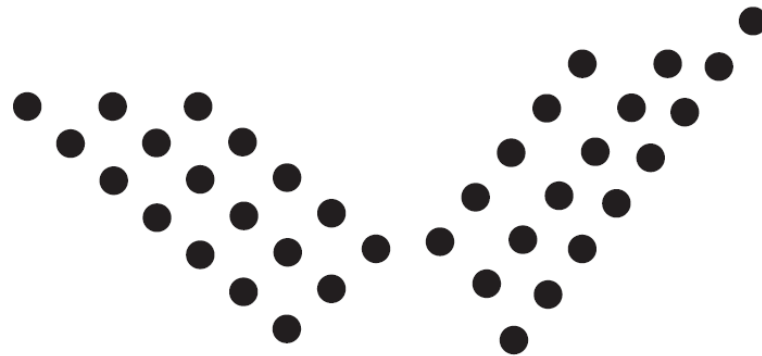
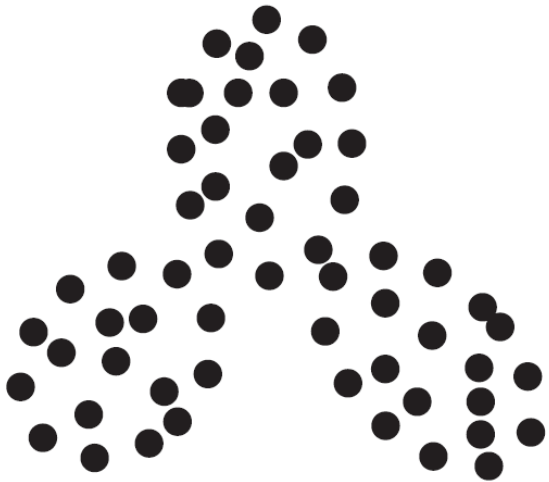
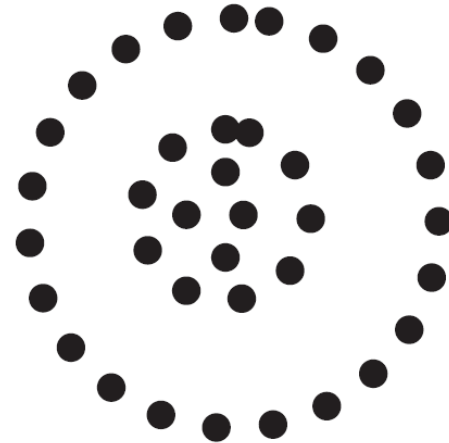
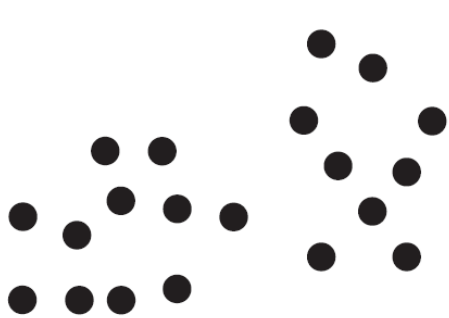
“ formal definition of cluster is not only difficult but may even be misplaced. ” (Everitt, 2001)

Collection of definitions (Everitt (1980)) :

- “ A cluster is a set of entities which are alike, and entities from different clusters are not alike. ” (**VAGUE!**)
- A cluster is “ an aggregate of points in the test space such that the distance between any two points in the cluster is less than the distance between any point in the cluster and any point not in it. ” (**TOO RESTRICTIVE!**)
- “ Clusters may be described as continuous regions of this space (d -dimensional feature space) containing a relatively high density of points, separated from other such regions by regions containing a relatively low density of points. ” (**COOL, BUT HOW TO COMPUTE DENSITY IN HIGH-DIMENSIONS?**)



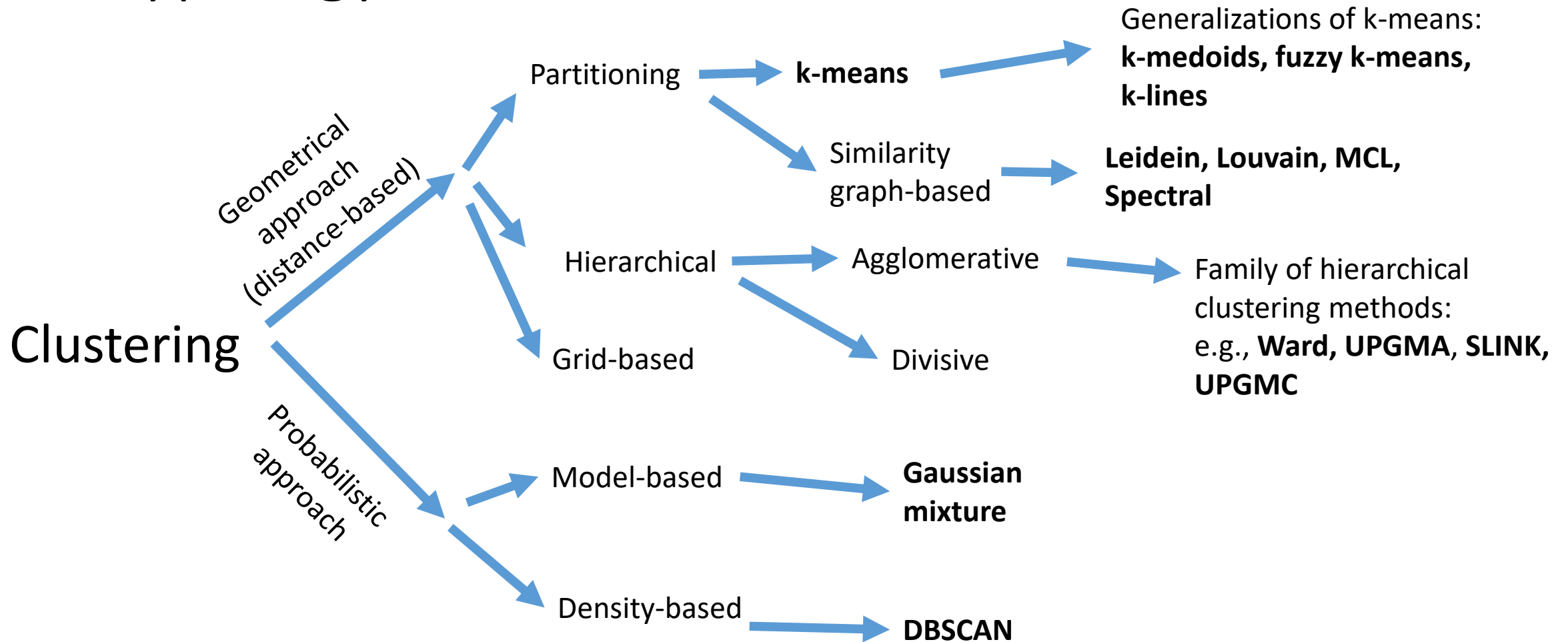
How many clusters?



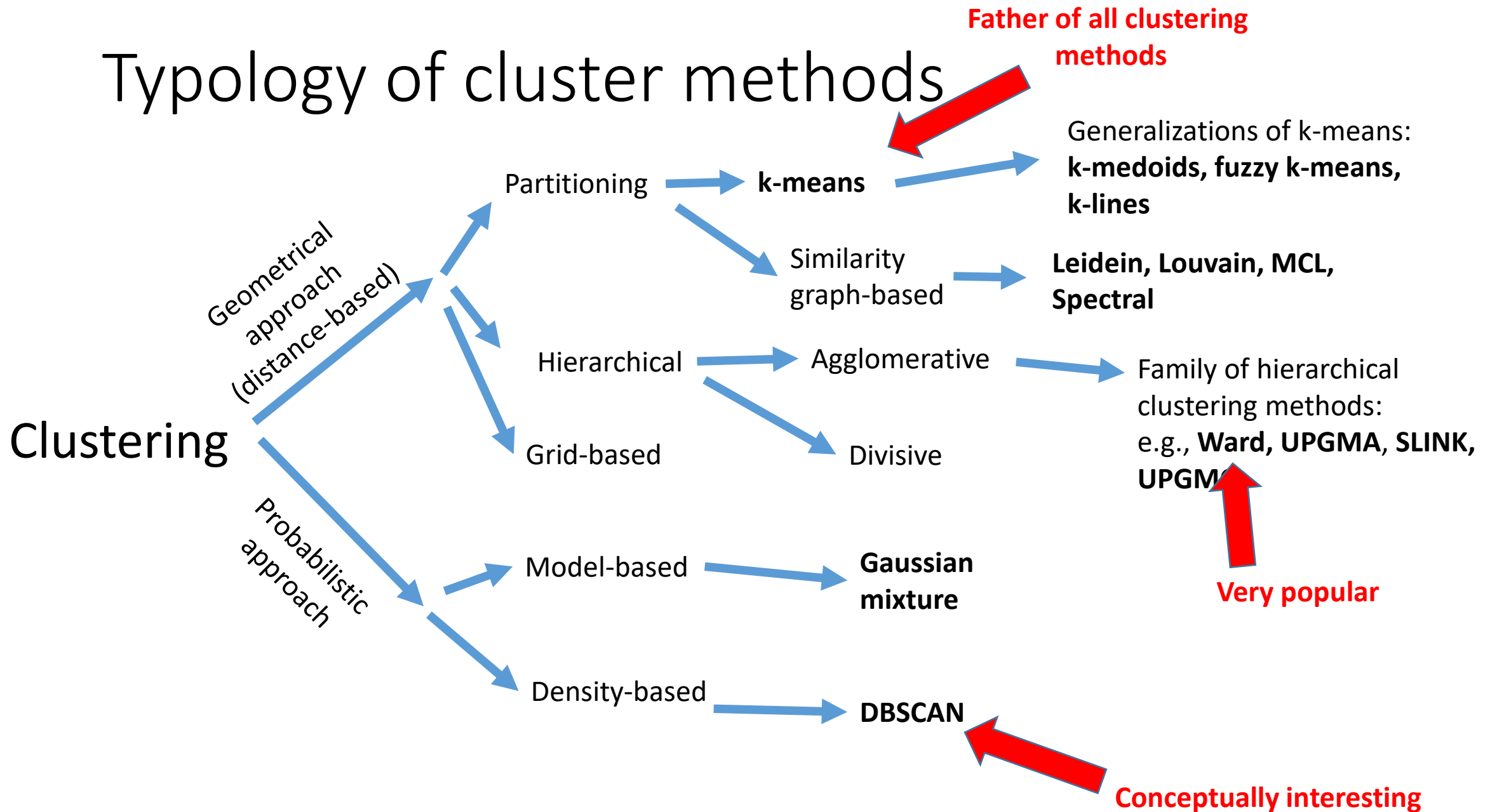
ANY clustering method requires specifying the number of clusters as a parameter

- Sometimes it is done explicitly
- Sometimes it is done through some kind of 'scale' or 'resolution' parameter

Typology of cluster methods



Typology of cluster methods



What you should ask about a clustering method

- | | |
|--------------|---|
| Base level | <ul style="list-style-type: none">• Input information (data table, distance table, KNN-graph, ...)• Computational complexity (time and memory requirements), scalability for big data ($O(K^r m^s N^p)$, K – number of clusters, m – number of dimensions, N – number of data points)• Constraints on cluster shapes (spherical, convex, ...)• Key parameters and requirements for domain knowledge to determine |
| Technicality | <ul style="list-style-type: none">• Possibility to work with various distance metrics• Sensitivity to noise and outliers• Ability to work in high-dimensional spaces |
| Flexibility | <ul style="list-style-type: none">• Ability for online learning• Incorporation of user-specified constraints• Interpretability and usability |

Solving clustering problem

